SEMICONDUCTOR

Use Of The $\mathrm{V}_{\mathrm{TO}}, \mathrm{r}_{\mathrm{T}}$ On-state Characteristic Model<br>Application Note<br>AN5001-1.1 June 1998

The use of the $\mathrm{V}_{\mathrm{TO}}, \mathrm{r}_{\mathrm{T}}$ on-state characteristic model and a more accurate alternative.

The inclusion of the theoretical terms $V_{T O}$ and $r_{T}$ in power semiconductor data sheets allows a simple means of calculating power loss, but this can lead to many incorrect assumptions. The terms in question are the two coefficients of a simple straight line model of the device on-state characteristic curve. To calculate the power the following formula is used:

$$
\begin{equation*}
P=V_{T 0} I_{T(A V)}+r_{T} k^{2} I_{T(A V)}{ }^{2} \tag{1}
\end{equation*}
$$

where k is the current waveform form factor, eg 1.57 for half sine wave.

The use of $\mathrm{V}_{\mathrm{TO}}$ and $\mathrm{r}_{\mathrm{T}}$ to approximate to the forward volt drop curve of a power semiconductor originates from pre-computer days when engineers used slide rules, calculators and, later on, simple computers for their calculations. The use of modern computers means that better approximations to the characteristic can easily be used. The most popular of these is the model proposed by General Electric:

$$
\begin{equation*}
V_{T M}=A+B^{\star}|n|+C^{*} \mid+D^{*} \operatorname{sqrt}(I) \tag{2}
\end{equation*}
$$

where $A, B, C$ and $D$ are constants with values specific to the device in question.


Fig. 1

The use of this model is described below.
$V_{T 0}, r_{T}$ Definitions
Although the straight line model is basically simple, variations in definition can lead to significant differences in calculated powers. Different manufacturers of power semiconductors have defined $V_{T 0}$ and $r_{T}$ in different ways. Here are 4 variations:

1) As Fig. 1, where the line is the tangent to the $V_{T M} v s I_{T}$ curve at the average current.
2) As Fig. 2, where a chord is drawn through $\mathrm{I}_{\mathrm{T}(\mathrm{AV})}$ and $3 \mathrm{xI}_{\mathrm{T}(\mathrm{AV}}$. This variation is the one used by Mitel for the calculation of data sheet power losses and current ratings. The definition is commonly used for thyristors. For rectifier diodes a chord through $3 \mathrm{x}_{\mathrm{T}(\mathrm{AV})}$ and $5 \mathrm{x}_{\mathrm{T}(\mathrm{AV})}$ sometimes gives a better result.
3) A variation of 2) which uses two straight lines instead of one to approximate to the true curve. In this version the lines pass through $1 / 6 \mathrm{I}_{\mathrm{T}(\mathrm{AV})}$ and $\pi \mathrm{I}_{\mathrm{T}(\mathrm{AV})}$ and also $\pi \mathrm{I}_{\mathrm{T}(\mathrm{AV})}$ and $20 \times \mathrm{I}_{\mathrm{T}(\mathrm{AV})}$.
4) As Fig 3. A tangential point constructed such that the value of $I_{\text {T(AV) }}$ calculated from:-

$$
\begin{equation*}
\mathrm{I}_{\mathrm{T}(\mathrm{AV})}=\left(-\mathrm{V}_{\mathrm{TO}} \pm \sqrt{ }\left(\mathrm{V}_{\mathrm{TO}}{ }^{2}+4^{*} \mathrm{k}^{2 *} r_{T}^{*} \mathrm{P}\right)\right) / 2^{*} \mathrm{k}^{2 \star} \mathrm{r}_{\mathrm{T}} \tag{3}
\end{equation*}
$$

is the same as that calculated by more exacting methods. This method is a variation of method 1). It has been used to retrospec-


Fig. 2


Fig. 3
tively calculate meaningful values of $\mathrm{V}_{\mathrm{T} 0}$ and $\mathrm{r}_{\mathrm{T}}$ where more accurate current rating data already exists.

## Limitations Of The $\mathrm{V}_{\mathrm{T} 0}, \mathrm{r}_{\mathrm{T}}$ Model

Using any one of the four definitions gives the correct value of the conduction losses at one or at most two points on the $\mathrm{V}_{\text {TM }}$ vs $\mathrm{I}_{\mathrm{T}}$ curve, ie where the straight line meets the true curve. It can be seen that depending on where a point is taken on the curve the answers will be optimistic or pessimistic. Definitions 1, 2 and 4 give adequate accuracy up to $3 \times \mathrm{I}_{\mathrm{T}(\mathrm{AV})}$.

For improved accuracy a mathematical model is needed which approximates better to the true curve.

## A Four Coefficient Model

The GE four term curve-fit equation given above has been shown to be a good isothermal approximation and is being increasingly adopted by several manufacturers of power semiconductors for inclusion in their datasheets. For the user, the one problem with the equation

$$
\begin{equation*}
\mathrm{V}_{T M}=\mathrm{A}+\mathrm{B}^{\star} \ln I+\mathrm{C}^{*} \mid+\mathrm{D}^{*} \operatorname{sqrt}(\mathrm{I}) \tag{2}
\end{equation*}
$$

is that, when multiplied by the equation for the current, it is not easily integratable to give the power loss. However, the equation is solvable by numerical integration, now easily possible with computers.

The following equation for half sine waves uses the $A, B, C$, $D$ coefficients used in the $\mathrm{V}_{\mathrm{TM}}$ equation above, their numerical values depending on the device type.

$$
\begin{equation*}
P=\left[A^{*}(I / E)+B^{*}(I / E)^{*} \ln (I / E)^{*} F+B^{*}(I / E)^{*} G+C^{*}(I / E)^{2} * H+D^{*}(I / E)^{3 / 2 *} J\right] \tag{4}
\end{equation*}
$$

where $I$ is the peak value of the half sine wave current.
The values of $\mathrm{E}, \mathrm{F}, \mathrm{G}, \mathrm{H}$ and J depend on the conduction angle and are given in the table 1, and for Rectangular waves :

$$
\begin{equation*}
\left.P=\left[A+B^{*} \ln \left(I^{*} 360 / \theta\right)+C^{*}\left(I^{*} 360 / \theta\right)+D^{*} \div\left({ }^{*} 360 / \theta\right)\right]^{*}\left(I^{*} 360 / \theta\right)\right] \tag{5}
\end{equation*}
$$

where $I$ is the average current (not the peak current) and q is the conduction angle in degrees.

Mitel has determined the values of $A, B, C$ and $D$ and these are given in the attached table 2.

| $C o n d u c t i o n ~ A n g l e ~$ <br> (degrees) | E | F | G | $\mathbf{H}$ | $\mathbf{J}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 180 | 1 | 0.31830986 | -0.0976260 | 0.25 | 0.27820862 |
| 120 | 1 | 0.23752350 | -0.0522407 | 0.02000795 | 0.21579720 |
| 90 | 0.75 | 0.15776190 | -0.0488128 | 0.12361100 | 0.13771530 |
| 60 | 0.45 | 0.08077821 | -0.0453849 | 0.04992036 | 0.06241130 |
| 30 | 0.067 | 0.02062772 | -0.0245605 | 0.00686488 | 0.01166912 |
| 15 |  | -0.0095093 | 0.00084797 | 0.00203133 |  |

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| Device Type Number | A | B | C | D |
| :---: | :---: | :---: | :---: | :---: |
| DCR504ST | 0.351374 | 0.171814 | 0.000964 | -0.020616 |
| DCR604SE | 1.086551 | -0.173031 | $-3.307461 \times 10^{-5}$ | 0.056345 |
| DCR803SG | 0.6102629 | 0.08049203 | 0.000249 | 0.005951 |
| DCR806SG | 0.6102629 | 0.08049203 | $7.189037 \times 10^{-4}$ | -0.01028328 |
| DCR818SG | 0.650046 | -0.018621 | 0.000589 | 0.063601 |
| DCR820SG | -0.759775 | 0.639225 | 0.004376 | -0.092153 |
| DCR1003SF | -1.191257 | 0.4149784 | $3.623888 \times 10^{-4}$ | -0.02991257 |
| DCR1006SF | -1.456962 | 0.5361379 | $6.639949 \times 10^{-4}$ | -0.04905585 |
| DCR1008SF | 1.458475 | -0.098355 | 0.000484 | 0.012565 |
| DCR1020SF | 0.25863 | 0.322589 | 0.002564 | -0.061059 |
| DCR1275SD | 1.255681 | -0.14019 | $7.581403 \times 10^{-5}$ | 0.025833 |
| DCR1277SD | 1.712517 | -0.201825 | 0.000256 | 0.025787 |
| DCR1279SD | 1.398966 | -0.078055 | 0.000504 | 0.011137 |
| DCR1374SBA | 0.4846543 | 0.05408984 | $8.508026 \times 10^{-5}$ | $1.863019 \times 10^{-3}$ |
| DCR1375SBA | 1.149986 | -0.09990939 | $7.993598 \times 10^{-5}$ | 0.02290949 |
| DCR1376SBA | 1.459103 | -0.07503561 | $3.442677 \times 10^{-4}$ | $7.82981 \times 10^{-4}$ |
| DCR1474SY | 0.7635305 | $8.73036 \times 10^{-3}$ | $8.568357 \times 10^{-5}$ | $1.537158 \times 10^{-3}$ |
| DCR1475SY | 1.259276 | -0.08537149 | $1.320759 \times 10^{-4}$ | $9.178437 \times 10^{-3}$ |
| DCR1476SY | 0.8659641 | 0.03698496 | $3.245389 \times 10^{-4}$ | $-2.597435 \times 10^{-3}$ |
| DCR1478SY | 0.8659641 | 0.03698496 | $3.245389 \times 10^{-4}$ | $-2.597435 \times 10^{-3}$ |
| DCR1574SY | 1.328994 | 0.1381631 | $3.565973 \times 10^{-6}$ | 0.01786171 |
| DCR1575SY | 1.659647 | -0.2206499 | $7.427997 \times 10^{-5}$ | 0.02837417 |
| DCR1576SY | 0.06963535 | 0.1224886 | $3.310485 \times 10^{-4}$ | $1.619778 \times 10^{-4}$ |
| DCR1594SW | 1.152158 | -0.08401428 | $3.351054 \times 10^{-5}$ | 0.01199439 |
| DCR1595SW | 0.02866651 | 0.1590393 | $1.947584 \times 10^{-4}$ | $-5.23298 \times 10^{-3}$ |
| DCR1596SW | -0.5011559 | 0.2638417 | $2.5367114 \times 10^{-4}$ | -0.01249303 |
| DCR1673SZ | 0.4769404 | 0.02958434 | $3.978298 \times 10^{-5}$ | $6.677479 \times 10^{-3}$ |
| DCR1674SZ | 0.6844942 | -0.0108645 | $7.203702 \times 10^{-5}$ | 0.01015201 |
| DCR1675SZ | 0.8497627 | -0.03614853 | $5.286579 \times 10^{-5}$ | 0.01334724 |

Table 2 List of thyristor GE $V_{T M}$ coefficients

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|  | Double Side Cooled |  |  | Single Side Cooled |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Device Type Number | $\begin{aligned} & \mathrm{I}_{\mathrm{T}(\mathrm{AV})} \\ & (\mathrm{A}) \end{aligned}$ | $\begin{aligned} & \mathrm{I}_{\text {TRMS }} \\ & (\mathrm{A}) \end{aligned}$ | $\begin{aligned} & \mathrm{I}_{\mathrm{DC}} \\ & \text { (A) } \end{aligned}$ | $\begin{aligned} & I_{T(A V)} \\ & (A) \end{aligned}$ | $\mathrm{I}_{\text {T(RMS) }}$ (A) | $\begin{aligned} & \mathrm{I}_{\mathrm{DC}} \\ & \text { (A) } \end{aligned}$ |
| DCR504ST | 354 | 556 | 497 | 246 | 387 | 320 |
| DCR604SE | 551 | 866 | 751 | 372 | 585 | 489 |
| DCR803SG | 817 | 1284 | 1088 | 506 | 795 | 636 |
| DCR806SG | 669 | 1051 | 928 | 428 | 672 | 552 |
| DCR818SG | 420 | 660 | 583 | 269 | 423 | 359 |
| DCR820SG | 310 | 487 | 447 | 204 | 321 | 279 |
| DCR1003SF | 1197 | 1881 | 1623 | 831 | 1305 | 1065 |
| DCR1006SF | 980 | 1540 | 1359 | 690 | 1083 | 900 |
| DCR1008SF | 828 | 1300 | 1164 | 585 | 920 | 774 |
| DCR1020SF | 514 | 807 | 765 | 377 | 592 | 530 |
| DCR1275SD | 1175 | 1846 | 1625 | 798 | 1255 | 1045 |
| DCR1277SD | 999 | 1570 | 1419 | 691 | 1086 | 922 |
| DCR1279SD | 859 | 1349 | 1217 | 593 | 932 | 787 |
| DCR1374SBA | 2102 | 3301 | 2773 | 1503 | 2361 | 1888 |
| DCR1375SBA | 1562 | 2453 | 2142 | 1139 | 1790 | 1501 |
| DCR1376SBA | 1319 | 2072 | 1851 | 975 | 1532 | 1298 |
| DCR1474SY | 2764 | 4342 | 3776 | 1729 | 2717 | 2175 |
| DCR1475SY | 2224 | 3494 | 3149 | 1431 | 2248 | 1877 |
| DCR1476SY | 1770 | 2780 | 2554 | 1155 | 1815 | 1542 |
| DCR1478SY | 1625 | 2553 | 2271 | 1035 | 1625 | 1345 |
| DCR1574SY | 2704 | 4247 | 3670 | 1682 | 2642 | 2144 |
| DCR1575SY | 2007 | 3153 | 2887 | 1307 | 2053 | 1772 |
| DCR1576SY | 1716 | 2695 | 2526 | 1140 | 1790 | 1578 |
| DCR1594SW | 3036 | 4769 | 4128 | 1894 | 2975 | 2407 |
| DCR1595SW | 2380 | 3739 | 3362 | 1532 | 2407 | 2014 |
| DCR1596SW | 2266 | 3560 | 3230 | 1469 | 2308 | 1950 |
| DCR1673SZ | 3625 | 5694 | 4956 | 2269 | 3565 | 2909 |
| DCR1674SZ | 3101 | 4871 | 4377 | 1991 | 3128 | 2640 |
| DCR1675SZ | 3029 | 4758 | 4223 | 1926 | 3025 | 2524 |

Table 3 List of GE calculated currents

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HEADQUARTERS POWER OPERATIONS
MITEL SEMICONDUCTOR
Doddington Road, Lincoln,
LN6 3LF, United Kingdom
Tel: + 44 (0)1522 500500
Fax: + 44 (0)1522 500550

Internet: http://www.mitelsemi.com
e-mail: power_solutions@mitel.com
POWER PRODUCT CUSTOMER SERVICE CENTRES

- FRANCE, BENELUX \& SPAIN Tel: + 33 (0)1 69189000 Fax : +33 (0)1 64465450
- NORTH AMERICA Tel: 011-800-5554-5554 Fax: 011-800-5444-5444
- UK, GERMANY, REST OF WORLD Tel: + $44(0) 1522500500$ Fax : + $44(0) 1522500020$

